

2/27/18 "Mistakes are the portal of Discovery." - James Joyce

HW: "Function Notation" HW
Test 2 on Friday 3/9

AIM: How do we evaluate functions?

Warm Up:

1) Express in simplest form, along with restrictions:

$x \neq -2$

$$\frac{\frac{x}{x+2}}{1 - \frac{x}{x+2}} = \frac{\frac{x}{x+2}}{\frac{x+2}{x+2} - \frac{x}{x+2}} = \frac{\frac{x}{x+2}}{\frac{2}{x+2}} = \frac{x}{2}$$

Handwritten work shows the simplification of the complex fraction:

$$\frac{\frac{x}{x+2}}{1 - \frac{x}{x+2}} = \frac{\frac{x}{x+2}}{\frac{x+2}{x+2} - \frac{x}{x+2}} = \frac{\frac{x}{x+2}}{\frac{2}{x+2}} = \frac{x}{2}$$

The final simplified form is $\frac{x}{2}$, with the restriction $x \neq -2$.

FUNCTION NOTATION

$$y = f(x)$$

Output $\xrightarrow{\quad}$ Rule $\xleftarrow{\quad}$ Input

Exercise #1: Evaluate each of the following given the function definitions and input values.

(a) $f(x) = 5x - 2$

(b) $g(x) = x^2 + 4$

$$f(3) = 5(3) - 2 = 13$$

$$g(3) = (3)^2 + 4 = 13$$

$$f(-2) = 5(-2) - 2 = -12$$

$$g(0) = (0)^2 + 4 = 4$$

$$f(x+1) = 5(x+1) - 2$$

$$= 5x + 5 - 2$$

$$= 5x + 3$$

$$g(a-2) =$$

$$= (a-2)^2 + 4$$

$$= a^2 - 4a + 4 + 4$$

$$= a^2 - 4a + 8$$

Exercise #2: Boiling water at 212 degrees Fahrenheit is left in a room that is at 65 degrees Fahrenheit and begins to cool. Temperature readings are taken each hour and are given in the table below. In this scenario, the temperature, T , is a function of the number of hours, h .

h (hours)	0	1	2	3	4	5	6	7	8
$T(h)$ (°F)	212	141	104	85	76	70	68	66	65

(a) Evaluate $T(2)$ and $T(6)$.

$$T(2) = 104$$

$$T(6) = 68$$

(b) For what value of h is $T(h) = 76$?

$$T(h) = 76$$

$$h = 4$$

(c) Between what two consecutive hours will $T(h) = 100$?

Between hours 2 and 3.

$$2 < h < 3$$

Exercise #3: The function $y = f(x)$ is defined by the graph shown below. Answer the following questions based on this graph.

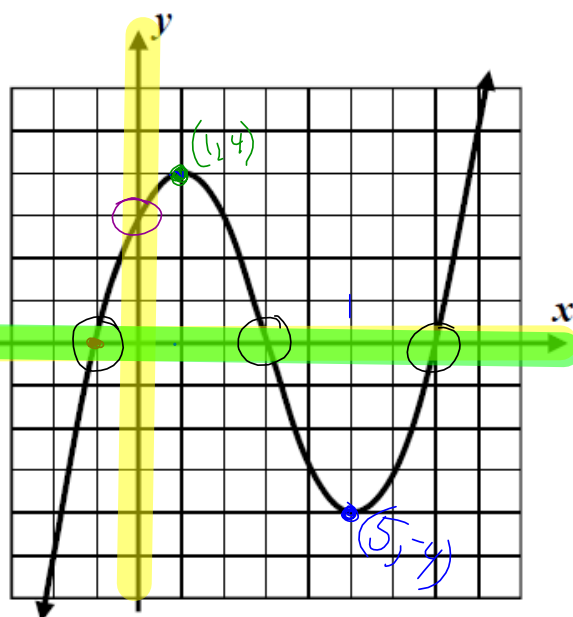
(a) Evaluate $f(-1)$, $f(1)$, and $f(5)$.

$f(-1)$ means "what is y -value when $x = -1$?"

$$f(-1) = 0$$

$$f(5) = -4$$

$$f(1) = 4$$



(b) Evaluate $f(0)$. What special feature on a graph does $f(0)$ always correspond to?

$$f(0) = 3 \quad \text{y-intercept}$$

(c) What values of x solve the equation $f(x) = 0$? What special features on a graph does the set of x -values that solve $f(x) = 0$ correspond to?

what is the x -value when $y = 0$?

- x -intercepts
- roots/zeros/solutions

$$@ x = -1, 3, 7$$

(d) Between what two consecutive integers does the largest solution to $f(x) = 3$ lie?